



Power Scheduling Of a Micro grid Using Direct Search Method

Shanthi.G, Dr.K.Elango

Department of EEE, Valliammai Engineering College, Kattangulathur, Chennai, India

Head of the Department, Department of EEE, Valliammai Engineering College, Kattangulathur, Chennai, India

Abstract- The objective is to minimize the fuel cost during the grid-connected operation, while ensuring stable operation after islanding. To achieve this goal, the economic dispatch (ED) problem and related constraints are formulated. The constraints considered in this study are: i) reserve for variation in load demand, ii) reserve for variation in the power outputs of non-dispatch able DGs, iii) flow limits between two adjacent areas, and iv) reserve for the stable islanded operation. The first three constraints, which have been employed in ED problem for conventional power systems, are modified to apply to Micro grids. We also provide a detailed formulation of the constraint for stable islanded operation in accordance with two power-sharing principles: i) fixed droop and ii) adjustable droop. The problem is solved using a modified direct search method, and the effect of the constraints on the operational cost is investigated via numerical simulations.

Index Terms—Distributed generator, economic dispatch, is-landed operation, microgrid, smart grid.

NOMENCLATURE

| | |
|-------------|---|
| g | Dispatchable DG unit index. |
| N_{gen} | Number of dispatchable units. |
| P_g | Power output of dispatchable unit g . |
| N_{ND} | Number of non-dispatchable units. |
| k | Non-dispatchable DG unit index. |
| P_{NDk} | Power output of non-dispatchable unit k . |
| $F_g(.)$ | Cost function of unit g . |
| P_g^{max} | Maximum generation limit of unit g . |

| | |
|------------------|--|
| P_g^{min} | Minimum generation limit of unit g . |
| d | Load index. |
| N_{load} | Number of loads. |
| LD_d | Power demand of load d . |
| P_{Main} | Power injected by the main grid. |
| P_{Ai} | Sum of power outputs of DGs in area i . |
| LD_{Ai} | Sum of load demands in area i . |
| FL_{i-j} | Power flow from area i to area j . |
| FL_{i-j}^{max} | Flow limit from area i to area j . |
| P_{Ai}^{min} | Sum of the minimum limits of the units in area i . |
| P_{Ai}^{max} | Sum of the maximum limits of the units in area i . |

I. INTRODUCTION

ELECTRIC power systems have been undergoing profound changes in response to various needs, such as environmental compliance, energy conservation, better grid reliability, improved operational efficiency, and customer ser-vice [1]. “Smart grid,” “intelligent grid,” and “next-generation grid” are the names applied to the power grid of the future, in which the electrical infrastructures and intelligent information networks will be integrated in order to satisfy the aforementioned needs [1]–[4]. In the meantime, the increasing use of distributed energy resources (DERs), including intermittent renewable sources, will pose many challenges for the future grid, especially with regard to the distribution system [1]. In order to solve the interconnection problems of individual distributed generators (DGs), the concept of a microgrid has been proposed [5]–[7]. A microgrid is a low- or medium - voltage distribution network, comprising various DGs, storage devices, and controllable loads, which can be



operated in either the grid- connected or islanded mode [5], [6]. To date, there have been numerous research projects on the design, control, and operation of micro grids throughout the world, such as the CERTS microgrid in USA [6], [7], the MICROGRID project of Europe [8], and the new energy integration test project carried

out by NEDO in Japan [9].

In [8] and [10]–[13], a central controller and an energy management system (EMS) were proposed as a means of deriving the greatest benefit from the operation of a microgrid, and increasing the efficiency of DG usage. The principal functions of a microgrid EMS are to provide power and voltage .

Among the above functions, this paper focuses on the problem of determining the power references of DGs for the optimal operation of a microgrid. The optimization of a micro-grid has important differences from the case of a large power system and its conventional economic dispatch (ED) problem [13]. One of the most important differences is the necessity for stable mode transition from a grid-connected to the islanded operation in case of grid faults. Therefore, we propose the formulations of the ED problem for micro grids and its related constraints, which yield the fuel cost minimization during the grid-connected operation while ensuring stable operation after islanding.

The remainder of this paper is divided into five sections. Section II introduces several issues regarding the power control of DGs in a microgrid. In Section III, the economic dispatch problem and related constraints are formulated for a microgrid. Section IV presents the formulation of the constraint for the stable islanded operation in accordance with the power-sharing principle between the DGs. Section V discusses the numerical simulation results which are utilized to investigate the effect of each constraint on the operational cost. Finally, Section VI contains some concluding remarks.

II. TECHNICAL ISSUES RELATED TO MICROGRID ED

A. Active Power and Frequency Control in a Microgrid

Before developing the formulation of the ED problem for a microgrid, we will briefly discuss some technical issues related to the active power and frequency control of DGs: 1) the power-control mode, 2) the power-sharing principle among DGs during microgrid islanding, and 3)

the controllability of energy sources.

1) *Power-Control Mode*: The power output of a DG can be controlled by one of two different modes: unit output power control (UPC) or feeder flow control (FFC) [7]. A UPC-mode DG generates constant active power according to the power reference, while the output of an FFC-mode DG is controlled so that the active power flow in the feeder remains constant. In this study, the power output reference for a UPC-mode DG and the feeder flow reference for an FFC-mode DG are determined by solving the ED problem regarding the optimal operation of a microgrid.

2) Power-Sharing Principle During Microgrid Islanding:

When a microgrid is disconnected from the main grid, DGs must take the place of the main grid in matching the power demand. In many studies, power versus frequency $P-f$ droop control has been adopted in order to ensure that the power demand is dynamically balanced by the DGs [5]–[8]. Conventionally, the droop constant of a DG is considered to be a fixed parameter, determined so that the load demand is shared among DGs in proportion to their rated capacities. In [15], a new power-sharing principle is proposed in which the droop constants are periodically modified according to the operating points of the DG units. With this method, the DGs share power according to their operational reserves, rather than their capacities. We refer to the former techniques as *fixed droop* and the latter techniques as *adjustable droop*, and formulate the constraint related to the islanded operation of a microgrid in accordance with the power-sharing principle.

3) *Controllability of Energy Sources*: The emerging generation technologies suitable for microgrid application, together

TABLE I
CHARACTERISTICS OF TYPICAL DG ENERGY SOURCES

| Energy source type | Capacity range | Dispatchability |
|--------------------------------|----------------|-----------------|
| Internal combustion engines | 10 kW ~ 10 MW | O |
| Small size combustion turbines | 0.5 ~ 50 MW | O |
| Microturbines | 20 ~ 500 kW | O |
| Fuel cells | 1 kW ~ 10 MW | O |
| Photovoltaic systems | 5 W ~ 5 MW | X |
| Wind turbines | 30 W ~ 10 MW | X |

With their typical capacity ranges, are listed in Table I [16]. Since most DGs are interfaced with the grid through an in-verter, they have various control capabilities, including power, frequency, and voltage

control. However, the power outputs of DGs with renewable energy sources, such as photovoltaic cells and wind turbines, are driven by weather, not by system loads [7]. Therefore, these intermittent sources cannot be used as dispatchable sources. In the ED problem, these sources will be treated as negative loads, and their power outputs will be assumed to be predictable within some range of uncertainty.

B. Constraints Associated With Microgrid Operation

As Fig. 1 indicates, the microgrid configuration considered in this study is a multiple-FFC configuration which is most suitable for a microgrid in which none of the DGs are dominant [17], [18]. We assume that the variation of loads and the power outputs of non-dispatchable DGs in each control area are compensated by the dispatchable DGs in the same area. To accomplish this, the first DG in each area operates in the FFC mode, while the others operate in the UPC mode, as shown in Fig. 1(b). With this configuration, any variation within an area can be compensated by the FFC-mode DG, and the flow between two adjacent areas remains unchanged over a predetermined time period [17]–[20]. This property is advantageous to system operators, since microgrids can be thought of as controllable subsystems.

The basic ED problem is extended to include the additional constraints related to the operation of a microgrid. The constraints considered in this study are as follows:

- i) Reserve for variation in load demand
- ii) Reserve for variation in the power outputs of non-dispatchable DGs
- iii) Flow limits between two adjacent areas
- iv) Reserve for the stable islanded operation.

Since the first three constraints have already been adopted as part of the ED problem for conventional power systems, they are simply modified for application to a microgrid. The unique constraint, concerning the reserve for the stable islanded operation, will be discussed in detail in Section IV.

III. ED PROBLEM FORMULATION FOR A MICROGRID

A. Formulation of the Basic ED Problem

In a power system, the primary objective of the ED is to minimize the total generation cost F_T , while

satisfying the power balance and generation limits of the units [21], [22]. This can be formulated as follows:

$$\min F_T = \sum_{g=1}^{N_{gen}} F_g(P_g) \quad (1)$$

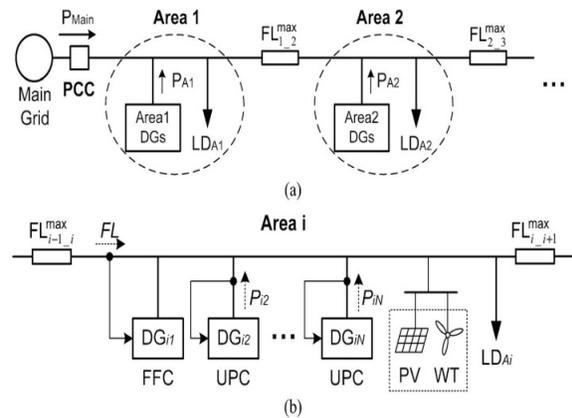


Fig. 1. Microgrid configuration. (a) Configuration of a microgrid with multiple control areas. (b) Configuration of a control area.

subject to Note that the power flow from/to the main grid P_{Main} is reflected by a decrease/increase in the load on the area nearest the

$$\sum_{g=1}^{N_{gen}} P_g = \sum_{d=1}^{N_{load}} LD_d \quad (2)$$

main grid (i.e., area 1), according to (7).

$$P_g^{min} \leq P_g \leq P_g^{max} \quad (3)$$

$$P_{Main} + FL_{1-2} = P_{A1} = LD_{A1} \quad (7)$$

B. Modification of the Constraint Formulations

$$= LD_{Ai} + FL_{i-i+1} - FL_{i-1-i} \quad (8)$$

Power Balance Constraints: The power balance condition $P_{A_n} = LD_{A_n} - FL_{n-1-n}$ (9) is modified as (4), taking into account the power outputs of the

$$\text{non-dispatchable sources and the power injected by the main grid} \quad -FL_{i-1-i}^{max} \leq FL_{i-1-i} \leq FL_{i-1-i}^{max} \quad (10)$$

The load demand and the power outputs of intermittent



IV. FORMULATION OF THE CONSTRAINT FOR THE STABLE

sources are assumed to be predicted for every time interval.

ISLANDED OPERATION

$$\sum_{g=1}^{N_{gen}} P_g + P_{main} = \sum_{d=1}^{N_{load}} LDD - \sum_{k=1}^{N_{nd}} P_{ndk} \quad (4)$$

Spinning Reserve Requirement Constraints:

When a microgrid is islanded, the DGs will adjust its power there are uncertainties involved in predicting wind velocity and/or irradiance. Moreover, load demand in order to compensate for the loss of the main grid. Since the power outputs of intermittent sources usually vary system topology is radial, a power output change from any DG continuously. In order to compensate for these variations, and will affect the power flow in the upstream lines. For example, to operate the system stably, additional reserve is necessary if power is imported from the main grid during the grid-connected and wind velocity and/or irradiance. Moreover, load demand operation, the DGs will increase their power outputs, and or a microgrid with the proposed configuration, in which all thus the upward flow in each line will be increased. Accordingly, the variations are picked up by the FFC-mode DG in each area, if the power flow between two areas has remained near its the constraint can be formulated as 5) and (6). The spinning maximum limit during the grid-connected operation power reserve requirement is reflected as a decrease in the maximum cannot be transmitted during the transition, and this can limit P_{max} and an increase in the minimum limit P_{min} of make the system unstable the first DG within each area. In this study, it is assumed that In [8] and [23], load shedding algorithms have been proposed the load demand varies within $r\%$ of the predicted value, and for stable operation in case of such contingencies. However, in the power outputs of the non-dispatch able sources vary within this paper, we assume that the DGs are capable of supplying all $u\%$ of the predicted value loads without curtailment during the islanded operation. For this

$$P_{i1} \leq P_{i1}^{max} - \left(\frac{r}{100} \sum_{d \in Ai} LDD + \frac{u}{100} \sum_{k \in Ai} P_{NDk} \right) \quad (5)$$

reason, the DGs should have at least as much reserve as

$$P_{i1} \geq + \left(\frac{r}{100} \sum_{d \in Ai} LDD + \frac{u}{100} \sum_{k \in Ai} P_{NDk} \right) \quad (6)$$

during the grid-connected operation. Furthermore, the inter-

3) Inter-Area Flow Limit Constrains:

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the power flow between two adjacent areas is restricted by the power output reference of the DGs. The more the flow limit physical limits. This constraint can be formulated as (7)-(10) the more stable the system will be when islanded. However, assuming that the number of areas in a feeder is n . such restriction will increase the operational cost during the grid-connected operation.

A. Constraint Formulation With Fixed Droop

With this power-sharing principle, each DG will change its power output in proportion to the inverse of the predetermined

$$\Delta P_g^{IM} = \frac{|1/Rg|}{\sum_{j=1}^{N_{gen}} \frac{1}{Rg}} \times (P_{main}) \quad (11)$$

Similarly, the amount of power shared by area i ΔP_{iM} can be calculated as the sum of the contributions for all the units in area i , as follows.

$$\Delta P_{Ai}^{IM} = \frac{\sum_{g \in Ai} |1/Rg|}{\sum_{j=1}^{N_{gen}} \frac{1}{Rg}} \times (P_{main}) \quad (12)$$

The constraints can be formulated differently, depending on whether the power is initially imported from or exported to the main grid.

1) *Power Initially Exported:* When the microgrid supplies power to the main grid during the grid-connected operation (i.e., $P_{Main} < 0$), the DGs will decrease their power outputs during the transition. Accordingly, all DGs should have additional down spinning reserve, and this is reflected by an increase in the minimum limit of the unit, as follows

$$P_g^{min} + \Delta P_g^{IM} \leq P_g \leq P_g^{max} \quad (13)$$

Since the DGs decrease their power outputs, the downward flow between areas will increase during the transition. Therefore, for the stable islanded operation without violating the physical inter-area flow limits, the downward flow should be maintained at an appropriate level below the limit during the grid-connected operation. The amount of additional flow from area $i-1$ to area i is the sum of the power shared by the DGs in area i and the areas downstream from it. Accordingly, the downward flow limit should be decreased by the amount of additional flow, whereas the upward flow limit remains unchanged.

$$-FL_{i-1-i}^{max} \leq FL_{i-1-i} \leq (FL_{i-1-i}^{max} - \sum_{a=i}^n \Delta P_{Aa}^{IM}) \quad (14)$$

2) *Power Initially Imported:* If power is imported from the main grid during the grid-connected operation, it should also be

$P > 0$),

Main

the DGs will increase their power outputs when the microgrid is disconnected from the main grid. Contrary to the former case, all DGs should have additional up spinning reserve, and the up-ward flow will be increased in the inter-area lines. Therefore, the

$$P_g^{min} \leq P_g \leq P_g^{max} - \Delta P_g^{IM} \quad (15)$$

$$(-FL_{i-1-i}^{max} - \sum_{a=i}^n \Delta P_{A_a}^{IM}) \leq FL_{i-1-i} \leq FL_{i-1-i}^{max} \quad (16)$$

Constraint Formulation With Adjustable Droop

When fixed droop is adopted, the contribution of each DG to the reserve is determined before solving the ED problem, and thus the output limit of a unit is modified according to (13) or (15). However, when adjustable droop is applied, the power output reference for each DG is determined optimally, and the contribution to the reserve is then determined according to its operational margin [14], [15]. Hence, the output limits of the DGs do not need to be modified. The inter-area flow limits, on the other hand, should be refined as in the case of fixed droop.

1) *Power Initially Exported:* As was noted in the fixed droop case, the DGs will decrease their power outputs in order to compensate for the loss of the main grid. If we assume that the output of unit g is P , the operational margin of this unit is $P - P_{min}$. Therefore, the power shared by unit g during the

transition (ΔP^{IM}) can be calculated as follows.

$$\Delta P_g^{IM} = \frac{P_g - P_g^{min}}{\sum_{j=1}^{N_{gen}(P_j - P_j^{min})} P_{A_i}} [P_{Main}] \quad (17)$$

As in the fixed droop case, the amount of power shared by area i ΔP^{IM} can be calculated as the sum of the contributions regarding all units in area.

$$\Delta P_{A_i}^{IM} = \frac{P_{A_i} - P_{A_i}^{min}}{\sum_{j=1}^{N_{gen}(P_j - P_j^{min})}} [P_{Main}] \quad (18)$$

The download flow limits should be decreased in a manner similar to (14). However, in this case, since the power shared by each unit is unknown until the ED problem is solved, the de-created value for the downward flow limits cannot be calculated directly as in the case of the fixed droop. The downward power flow from area $i-1$ to area i during the grid-connected operation is the sum of the differences between the load demands and power outputs of area i and the areas

downstream from it.

$$FL_{i-1-i} = \sum_{a=i}^n (LD_{A_a} - P_{A_a}) \quad (19)$$

The additional flow in the line between area $i-1$ and area i during the transition (ΔFL_{i-1-i}) can be calculated as follows.

$$\Delta FL_{i-1-i} = \sum_{a=i}^n \Delta P_{A_a}^{IM} = \frac{\sum_{a=i}^n P_{A_a} - \sum_{a=i}^n P_{A_a}^{min}}{\sum_{g=1}^{N_{gen}(P_g - P_g^{min})}} |P_{Main}| \quad (20)$$

Using the power balance equation given in (4), the denominator of the right-hand side of (20) can be rewritten as in (21). For the sake of simplicity, it is assumed that the power outputs of the non-dispatchable DGs are included in the load as negative values

$$\sum_{g=1}^{N_{gen}} (P_g - P_g^{min}) = \sum_{d=1}^{N_{load}} LD_{d+} + |P_{Main}| - \sum_{g=1}^{N_{gen}} P_g^{min} \quad (21)$$

V. NUMERICAL SIMULATIONS AND RESULTS

TABLE II

COST DATA FOR A 15 UNIT TEST SYSTEM

| Area | DG | Mode | Cost data | | | Output limit(kW) | |
|-------|-----|------|-----------|--------|--------|------------------|-----------|
| | | | a_g | b_g | c_g | p^{max} | p^{min} |
| Area1 | G1 | FFC | 14.526 | 0.1032 | 0.0001 | 300 | 35 |
| | G2 | UPC | 5.0797 | 0.0792 | 0.0005 | 100 | 20 |
| | G3 | UPC | 8.7657 | 0.0656 | 0.0004 | 150 | 30 |
| | G4 | UPC | 0.8505 | 0.0689 | 0.0009 | 80 | 10 |
| | G5 | UPC | 2.0491 | 0.0301 | 0.0011 | 100 | 20 |
| Area2 | G6 | FFC | 8.5957 | 0.0346 | 0.0002 | 250 | 60 |
| | G7 | UPC | 0.8505 | 0.0689 | 0.0009 | 80 | 10 |
| | G8 | UPC | 5.0797 | 0.0792 | 0.0005 | 100 | 20 |
| | G9 | UPC | 3.4047 | 0.0134 | 0.0009 | 120 | 30 |
| | G10 | UPC | 3.4047 | 0.0134 | 0.0009 | 120 | 30 |
| Area3 | G11 | FFC | 14.526 | 0.1032 | 0.0001 | 300 | 35 |
| | G12 | UPC | 5.4976 | 0.1164 | 0.0002 | 150 | 20 |
| | G13 | UPC | 5.4976 | 0.1164 | 0.0002 | 150 | 20 |
| | G14 | UPC | 1.0171 | 0.0486 | 0.0013 | 75 | 10 |
| | G15 | UPC | 3.5442 | 0.1189 | 0.0003 | 100 | 10 |
| Total | | | | | | 2175 | 360 |

TABLE III

DAILY LOAD PATTERN OF THE TEST SYSTEM

| Hour | Load (kW) | Hour | Load (kW) |
|--------|-----------|---------|-----------|
| 1 ~ 4 | 1,250 | 13 ~ 16 | 1,350 |
| 5 ~ 8 | 1,100 | 17 ~ 20 | 1,500 |
| 9 ~ 12 | 1,200 | 21 ~ 24 | 1,400 |

A test system comprising three control areas is utilized for the analysis. We assume that five DGs are installed in each area; the cost data of the DGs and the daily load demands are summarized in Tables II and III, respectively. We also assume that the load demands in Table III include the effects of non-dispatchable DGs, for simplicity. Since the effect of each constraint on the

cost varies according to the load distribution, we tested two cases in regards to each condition.

Case 1) Load distribution factor of each area=0.35:0.25:

0.40

Case 2) Load distribution factor of each area=0.30:0.35:

0.35

Various mathematical approaches and optimization techniques have been developed for solving ED problems. Chen proposed a direct search method (DSM) for an ED problem with transmission constraints [27], and applied it to ED problems with various types of constraints, such as wind-thermal coordination dispatch and generation-reserve dispatch [28], [29]. In this study, the DSM is applied (with some modifications) in order to solve the ED problem for microgrids, since it offers these definite advantages: i) the algorithm is straightforward and easy to implement, and ii) various inequality and equality constraints can be included. A multi-level convergence strategy, proposed in [27], is also used to improve the performance of the DSM.

B. Test 1: Inter-Area Flow Limit and Load Variation

The first simulation was designed to investigate the effect of the inter-area flow limit and the load variation on generation cost. To accomplish this, the total fuel cost was calculated under various conditions of load distribution, reserve requirement, and inter-area flow limit. The amount of power injected by the main

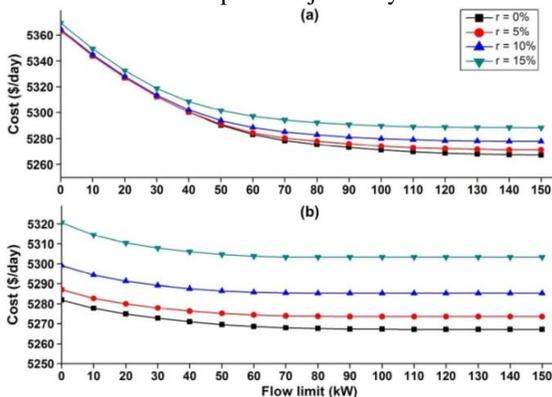


Fig. 2. Effects of inter-area flow limit and load variation reserve. (a) Results for Case 1. (b) Results for Case 2.

grid, P_{Main} , was assumed to be 0 in this test. The daily fuel costs in terms of the different conditions for the two cases are summarized in Fig. 2.

The effects of both factors on cost can be summarized as follows. Generation cost increased as the inter-area flow limit became smaller, and this occurred because units with higher incremental cost should increase their outputs as the flow limit decreases. In the test system, the DGs in area 2 had relatively lower incremental cost, but the load level of this area in Case 1 was only 25% of the total demand. Therefore, in order to reduce the total generation cost, the DGs in area 2 should produce more power than the local load demand, and transfer the surplus power to other areas. For example, at a system load of 1500 kW, approximately 22 kW and 118 kW of power were transferred from area 2 to areas 1 and 3, respectively, when the inter-area flow was not limited. However, as the inter-area flow limit decreases, the power transferred from area 2 is restricted, and the units in areas 1 and 3 with higher incremental cost should increase their outputs, which also increases the total generation cost.

We can also see that the cost showed a tendency to increase with the reserve requirement regarding load variation. The power output for the FFC-DGs in each area should be restricted in order to compensate for load variation, in accordance with

(5) and (6). Since the incremental costs of the FFC DGs were relatively lower, an increase in the reserve requirement resulted in higher generation cost. Another observation from Fig. 2 is that the effect of the inter-area flow limit was dominant in Case 1, while the effect of load variation reserve was critical in Case 2.

C. Test 2: Reserve for the Stable Islanded Operation

The effect of the reserve for the stable islanded operation was investigated by simulation under various load levels and P_{Mi} . We tested the following three conditions with differing load distributions and/or FL_{max} values, and P_{Main} was varied from

- 100 to 100 kW in 10 kW steps for each condition.
- Condition 1) Load distribution of Case 1 and $FL_{max} = 40$ kW
- Condition 2) Load distribution of Case 2 and $FL_{max} = 40$ kW
- Condition 3) Load distribution of Case 1 and $FL_{max} = 80$ kW

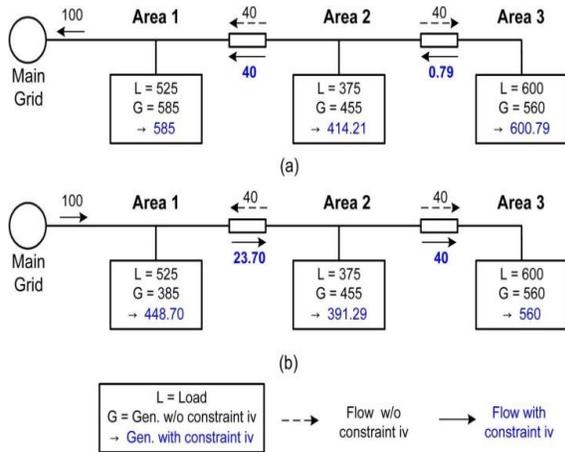


TABLE IV
APPROXIMATED PART-LOAD EFFICIENCY DATA
FOR THE DGS
SIMULATION RESULT FOR IMPORT, EXPORT,
& ISLAND

| AREA | PG | IMPORTED | | EXPORTED | | ISLANDING | | |
|-------|-----|----------------------|-------------------|----------------------|-------------------|----------------|-------------------|--------|
| | | 100 KW IMPORTED (KW) | FUEL COST (\$/KW) | 100 KW EXPORTED (KW) | FUEL COST (\$/KW) | ISLANDING (KW) | FUEL COST (\$/KW) | |
| 1 | P1 | 225.75 | 42.92 | 284.62 | 52.00 | 255.18 | 47.37 | |
| | P2 | 64.57 | 12.28 | 72.42 | 13.44 | 68.49 | 12.85 | |
| | P3 | 97.71 | 18.99 | 107.52 | 20.44 | 102.61 | 19.71 | |
| | P4 | 41.59 | 5.27 | 45.95 | 5.92 | 43.77 | 5.59 | |
| | P5 | 51.67 | 6.54 | 55.23 | 7.07 | 53.45 | 6.80 | |
| TOTAL | | 481.28 | | 565.75 | | 523.51 | | |
| 2 | P6 | 250.00 | 29.75 | 250.00 | 29.75 | 250.00 | 29.75 | |
| | P7 | 41.59 | 5.27 | 45.95 | 5.92 | 43.77 | 5.59 | |
| | P8 | 64.57 | 12.28 | 72.42 | 13.44 | 68.49 | 12.85 | |
| | P9 | 72.43 | 9.10 | 76.79 | 9.74 | 74.61 | 9.41 | |
| | P10 | 72.43 | 9.10 | 76.79 | 9.74 | 74.61 | 9.41 | |
| TOTAL | | 501.01 | | 521.94 | | 511.88 | | |
| 3 | P11 | 202.83 | 39.57 | 242.08 | 45.37 | 222.46 | 42.43 | |
| | P12 | 68.42 | 14.40 | 88.04 | 17.30 | 78.23 | 15.83 | |
| | P13 | 68.42 | 14.40 | 88.04 | 17.30 | 78.23 | 15.83 | |
| | P14 | 36.60 | 4.54 | 39.62 | 4.98 | 38.11 | 4.76 | |
| | P15 | 41.44 | 8.99 | 54.53 | 10.92 | 47.99 | 9.94 | |
| TOTAL | | 417.71 | | 233.39 | 512.31 | 263.31 | 465.01 | 248.12 |

Fig. 3. Sampled result for Condition 1 at load demand = 1500kW. (a) 100 kW is exported. (b) 100 kW is imported.

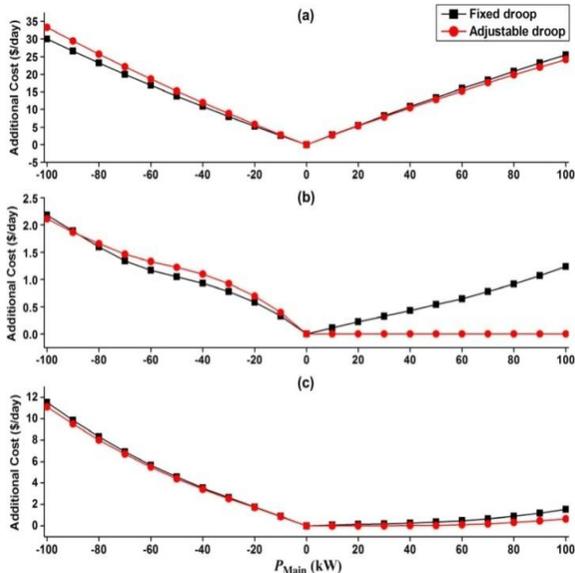


Fig. 4. Additional cost due to the reserve for the stable islanded operation. (a) Results for condition 1. (b) Results for condition 2. (c) Results for condition 3.

| AREA | PG | IMPORTED | | EXPORTED | | ISLANDING | | |
|-------|-----|----------------------|-------------------|----------------------|-------------------|----------------|-------------------|--------|
| | | 100 KW IMPORTED (KW) | FUEL COST (\$/KW) | 100 KW EXPORTED (KW) | FUEL COST (\$/KW) | ISLANDING (KW) | FUEL COST (\$/KW) | |
| 1 | P1 | 225.75 | 42.92 | 284.62 | 52.00 | 255.18 | 47.37 | |
| | P2 | 64.57 | 12.28 | 72.42 | 13.44 | 68.49 | 12.85 | |
| | P3 | 97.71 | 18.99 | 107.52 | 20.44 | 102.61 | 19.71 | |
| | P4 | 41.59 | 5.27 | 45.95 | 5.92 | 43.77 | 5.59 | |
| | P5 | 51.67 | 6.54 | 55.23 | 7.07 | 53.45 | 6.80 | |
| TOTAL | | 481.28 | | 565.75 | | 523.51 | | |
| 2 | P6 | 250.00 | 29.75 | 250.00 | 29.75 | 250.00 | 29.75 | |
| | P7 | 41.59 | 5.27 | 45.95 | 5.92 | 43.77 | 5.59 | |
| | P8 | 64.57 | 12.28 | 72.42 | 13.44 | 68.49 | 12.85 | |
| | P9 | 72.43 | 9.10 | 76.79 | 9.74 | 74.61 | 9.41 | |
| | P10 | 72.43 | 9.10 | 76.79 | 9.74 | 74.61 | 9.41 | |
| TOTAL | | 501.01 | | 521.94 | | 511.88 | | |
| 3 | P11 | 202.83 | 39.57 | 242.08 | 45.37 | 222.46 | 42.43 | |
| | P12 | 68.42 | 14.40 | 88.04 | 17.30 | 78.23 | 15.83 | |
| | P13 | 68.42 | 14.40 | 88.04 | 17.30 | 78.23 | 15.83 | |
| | P14 | 36.60 | 4.54 | 39.62 | 4.98 | 38.11 | 4.76 | |
| | P15 | 41.44 | 8.99 | 54.53 | 10.92 | 47.99 | 9.94 | |
| TOTAL | | 417.71 | | 233.39 | 512.31 | 263.31 | 465.01 | 248.12 |



| DG | Unit efficiency data | | | | | | Output limit | | |
|-------|----------------------|----------|----------|----------|----------|----------|--------------|-----------|-----|
| | e_{1g} | e_{2g} | e_{3g} | e_{4g} | e_{5g} | e_{6g} | p^{max} | p^{min} | |
| Area1 | 1 | 0.0607 | 0.5612 | -0.4043 | -0.4623 | 0.9022 | -0.3912 | 300 | 35 |
| | 2 | 0.0636 | 0.9291 | -2.3309 | 3.4601 | -2.5667 | 0.7247 | 100 | 20 |
| | 3 | 0.071 | 0.5177 | -0.4007 | -0.0287 | 0.2003 | -0.0795 | 150 | 30 |
| | 4 | 0.3747 | 0.4623 | -2.0704 | 3.6503 | -2.9996 | 0.9033 | 80 | 10 |
| | 5 | 0.0883 | 0.8003 | -2.0221 | 3.0601 | -2.3549 | 0.6985 | 100 | 15 |
| Area2 | 6 | 0.0607 | 0.5612 | -0.4043 | -0.4623 | 0.9022 | -0.3912 | 300 | 35 |
| | 7 | 0.0913 | 0.4694 | -0.1085 | -1.0011 | 1.3561 | -0.5372 | 150 | 20 |
| | 8 | 0.3747 | 0.4623 | -2.0704 | 3.6503 | -2.9996 | 0.9033 | 80 | 10 |
| | 9 | 0.0636 | 0.9291 | -2.3309 | 3.4601 | -2.5667 | 0.7247 | 100 | 20 |
| | 10 | 0.3717 | 0.0608 | 0.5602 | -2.1454 | 2.4131 | -0.9356 | 120 | 30 |
| Area3 | 11 | -0.0822 | 2.969 | -7.9065 | 10.936 | -7.6061 | 2.0994 | 200 | 60 |
| | 12 | 0.3717 | 0.0608 | 0.5602 | -2.1454 | 2.4131 | -0.9356 | 120 | 30 |
| | 13 | 0.0913 | 0.4694 | -0.1085 | -1.0011 | 1.3561 | -0.5372 | 150 | 20 |
| | 14 | 0.3547 | 0.5367 | -1.7736 | 2.3437 | -1.5412 | 0.3854 | 75 | 10 |
| | 15 | 0.3547 | 0.5367 | -1.7736 | 2.3437 | -1.5412 | 0.3854 | 75 | 10 |
| Total | | | | | | | | 2100 | 350 |

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VI CONCLUSION

The economic dispatch problem was formulated in accordance with various constraints related to the operation of a microgrid. Some constraints were formulated by modifying existing constraints to fit the configuration of a microgrid. We proposed an additional constraint to ensure the stable islanded operation of a microgrid, and provided a detailed formulation according to the power-sharing principle regarding the DGs. A test system with 15 DG units was developed for numerical simulations, taking into account the source type and part-load performance of each DG. We then investigated the effect of various parameters (including reserve requirement for the load variation, flow limit, load distribution pattern, and the power injected by the main grid) on the cost. Although the cost increased by up to 0.7%, a microgrid could be operated economically during the grid-connected mode, and soundly during the islanded mode, using the modified dispatch solution, which takes into account the additional con

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